

Probabilistic Refinement

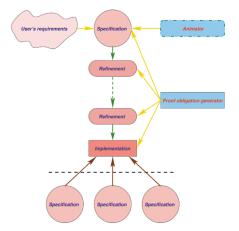
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Our aim is to produce a theoretical method, and associated tools, that will increase the rigour with which designers can incorporate the probabilistic information necessary to quantify risk and expected cost-of-failure in embedded computer systems.

 $B \ Method \ (B)$ is a formal development method that facilitates the refinement of specification to code.



Probabilistic B

Our probabilistic B (pB) replaces Boolean by real valued probabilities in the range 0..1. This allows probabilistic uncertainty to be modelled.

Probabilistic choice

$$S_p \oplus T$$

represents a choice between S and T in which S is taken with probability p and T is taken with probability 1-p.

Questions?

- \star What is the expected running cost of a system?
- * What is the reliability for a system given some information about its component?

Example The following illustrates a simple library in which books are lost with probability p.

StartLoan $\hat{=}$

```
\begin{array}{ll} \mathbf{pre} & booksInLibrary > 0 & \mathbf{then} \\ & booksInLibrary := booksInLibrary - 1 & \| \\ & loansStarted := loansStarted + 1 \\ \mathbf{end} \end{array}
```

FndLoan ≘

```
\begin{array}{ll} \textbf{pre} & loansEnded < loansStarted & \textbf{then} \\ & booksLost := booksLost + 1 \underset{p \oplus}{} booksInLibrary := booksInLibrary + 1 & \| \\ & loansEnded := loansEnded + 1 \end{array}
```

end

Invariants are replaced by *expectations*. For this specification, the expectation is defined by

$$E \mathrel{\widehat{=}} p*loansEnded-booksLost \ .$$

We can conclude that the expected number of books lost is bounded above by p * loansEnded.

Current status

The extended B (pB) and modified B-Toolkit supports the following:

- * Probabilistic invariant;
- * Probabilistic specification substitution;
- * Termination with probability 1;
- * Fundamental theorem for refinement;
- * Probabilistic loops.

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