

PS2 QFT3

(Due date - April 16, 2015)

1. a) Use the power-counting argument to construct counterterms and draw all the one-loop divergent 1PI graphs for real scalar theory

$$\mathcal{L}_{int} = -\frac{\lambda_1}{3!} \phi^3 - \frac{\lambda_2}{4!} \phi^4 \quad [3]$$

b) Use the power-counting argument to construct counterterms for the QED

$$\mathcal{L} = \bar{\psi} (i \gamma^\mu \partial_\mu - m) \psi - e \bar{\psi} \gamma^\mu \psi A_\mu - \frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

where  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$  [3]

2. Consider  $\lambda\phi^3$  theory in  $n$ -dimensions [2]

$$\mathcal{L} = \frac{1}{2} (\partial_\mu \phi)^2 - \frac{m^2}{2} \phi^2 - \frac{\lambda_0}{3!} \phi^3$$

a) Show that  $\lambda_0$  has  $\frac{6-n}{2}$  dimension [1] in  $n$ -dimensional space-time.

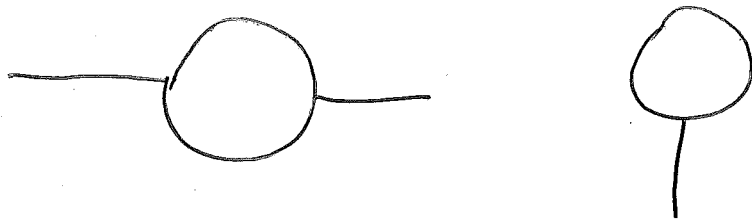
To have  $\lambda_0$  with fixed dimension for arbitrary  $n$ , we can define

$$\bar{\lambda}_0 = \lambda_0(\mu)^{\frac{4-n}{2}} = \lambda_0 \mu^\epsilon, \quad \epsilon = \frac{4-n}{2}$$

where  $\mu$  is an arbitrary mass scale

b) Show that one-loop divergent graphs for  $n=4$  are given

[3] by



c) Carry out renormalization for this theory using  $\overline{MS}$  scheme

[10]